

EXAM 8 – FALL 2011

20. (2.5 points)

The following information is known about a balanced retrospectively rated policy:

Losses at minimum premium	\$150,000
Losses at maximum premium	\$400,000
Loss conversion factor	1.20
Basic premium	\$50,000

- There is a 10% chance that this policyholder has no losses.
- There is a 90% chance that the losses are uniformly distributed between \$0 and \$500,000.
- There are no taxes.

Calculate the guaranteed cost premium for this policy.

Question 20

Sample 1

Losses @ Min= \$150,000

Losses @ Max= \$400,000

$$E[\text{Ground Up Loss}] = 0.1 * 0 + 0.9 * 250,000 = 225,000$$

$$\begin{aligned} E[L] &= \text{Expected losses entering retro formula} \\ &= 0.1 * 150,000 + .9 * [.3 * 150,000 + 0.2 * 400,000 + 0.5 * [(150,000 + 400,000)/2]] \\ &= 251,250 \end{aligned}$$

$$\begin{aligned} \text{Expected Retro Premium} &= (b + c * E[L])T \\ &= (50,000 + 1.2 * 251,250) = 351,500 \end{aligned}$$

Guaranteed cost premium = expected retro premium in a balanced plan.

Sample 2

$$E[A] = 0.9 * 250,000 = 225,000$$

Insurance Charge

$$\text{Above Max} = (500k - 400k)/2 * 0.2 * 0.9 = 9,000$$

$$\text{Below Min} = [(150k - 0)/2 * 0.3 * 0.9] + 150k * 0.1 = 35,250$$

$$\text{Converted Insurance Charge} = 1.2 * (9,000 - 35,250) = -31,500$$

$$b = e - (c-1)E + cl$$

$$\begin{aligned} e+E &= (b + cE - cl)*T \\ &= 50,000 + 1.2 * 225,000 - (-31,500) \\ &= 351,500 \end{aligned}$$

The plan is balanced, so GCP = e+E = 351,500.