EXAM 8 – FALL 2011

25. (1.5 points)

The following information is available for a retrospectively rated policy:

Standard premium	\$20,000
Guaranteed cost premium	\$19,760
Provisions for losses and expenses exclusive of taxes	\$19,160
Expected losses	\$12,000
Loss conversion factor	1.250
Tax multiplier	1.025
Selected maximum loss ratio	95%
Selected minimum loss ratio	20%
Charge for maximum	0.055
Charge for minimum	0.700

Calculate the maximum premium ratio for this policy.

Question 25

Sample 1

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\begin{array}{l} X_H - X_G = (e + E - H/T)/cE \\ 0.7 - 0.055 = (19,160/20,000 - H/1.025)/1.25*0.6 \\ H = 0.4861 \\ r_G = 0.95/0.6 = 1.583 \\ r_H = 0.2/0.6 = 0.333 \\ r_G - r_H = (G - H)/cET \\ 1.583 - 0.333 = (G - 0.4861)/1.25*1.025*0.6 \\ G = 1.447 \\ \hline \\ \textbf{Sample 2} \\ \Psi(r_H) = 0.7 + 0.2/0.6 - 1 = 0.033 \\ GCP = T(e + E) \\ 19,760/20,000 = 0.988 = 1.025(e + 0.6) \\ \end{array}
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19,760/20,00 e = 0.3639

E = 12/20 = 0.6

I = 0.6(0.055 - 0.033) = 0.013

b = e - (c-1)E + cI = 0.3639 - 0.25(0.6) + 1.25(0.013) = 0.2302

 $G = (b+cr_G E)T$

 $r_G = 0.95/0.6 = 1.583$

G = (0.2302 + 1.25*1.583*0.6)*1.025 = 1.4531

Sample 3

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\begin{split} & \mathsf{GCP} = 19,760 = (e+E)\mathsf{T} \\ & e+E = 19,160 \\ & \mathsf{E} = 12,000 \\ & e = 7,160 \\ & \mathsf{T} = 19,760/19,160 = 1.0313 \\ & \mathsf{B} = e - (c-1)\mathsf{E} + c\mathsf{I} \\ & \mathsf{cI} = c(\mathsf{X}_\mathsf{G} - \mathsf{S}_\mathsf{H})\mathsf{E} \\ & \mathsf{b} = 7,160 - 0.25*12,000+1.25(0.055 - 0.0333)*12,000 = 4,485 \\ & \mathsf{X}_\mathsf{G} = 0.055 \\ & \mathsf{X}_\mathsf{H} = 0.700 \\ & \mathsf{S}_\mathsf{H} = \mathsf{X}_\mathsf{H} + \mathsf{r}_\mathsf{H} - 1 = 0.7 + 1/3 - 1 = 0.03333 \\ & \mathsf{r}_\mathsf{H} = \mathsf{L}_\mathsf{H}/\mathsf{L} = 0.2*\mathsf{SP}/12,000 = 4,000/12,000 = 1/3 \\ & \mathsf{G} = (b+\mathsf{L}_\mathsf{G}\mathsf{c})\mathsf{T} = (4485 + 19,000*1.25)*1.0313 = 29,119 \\ & \mathsf{L}_\mathsf{G} = 0.95*\mathsf{SP} = 19,000 \\ & \mathsf{G} \text{ ratio} = 29,119/\mathsf{SP} = 1.456 \end{split}
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